

Probabilistic Robotics

SLAM

The SLAM Problem

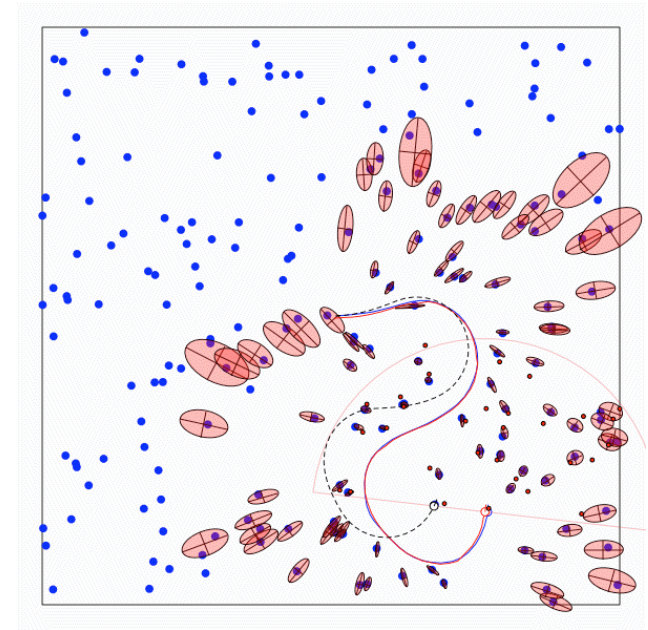
A robot is exploring an unknown, static environment.

Given:

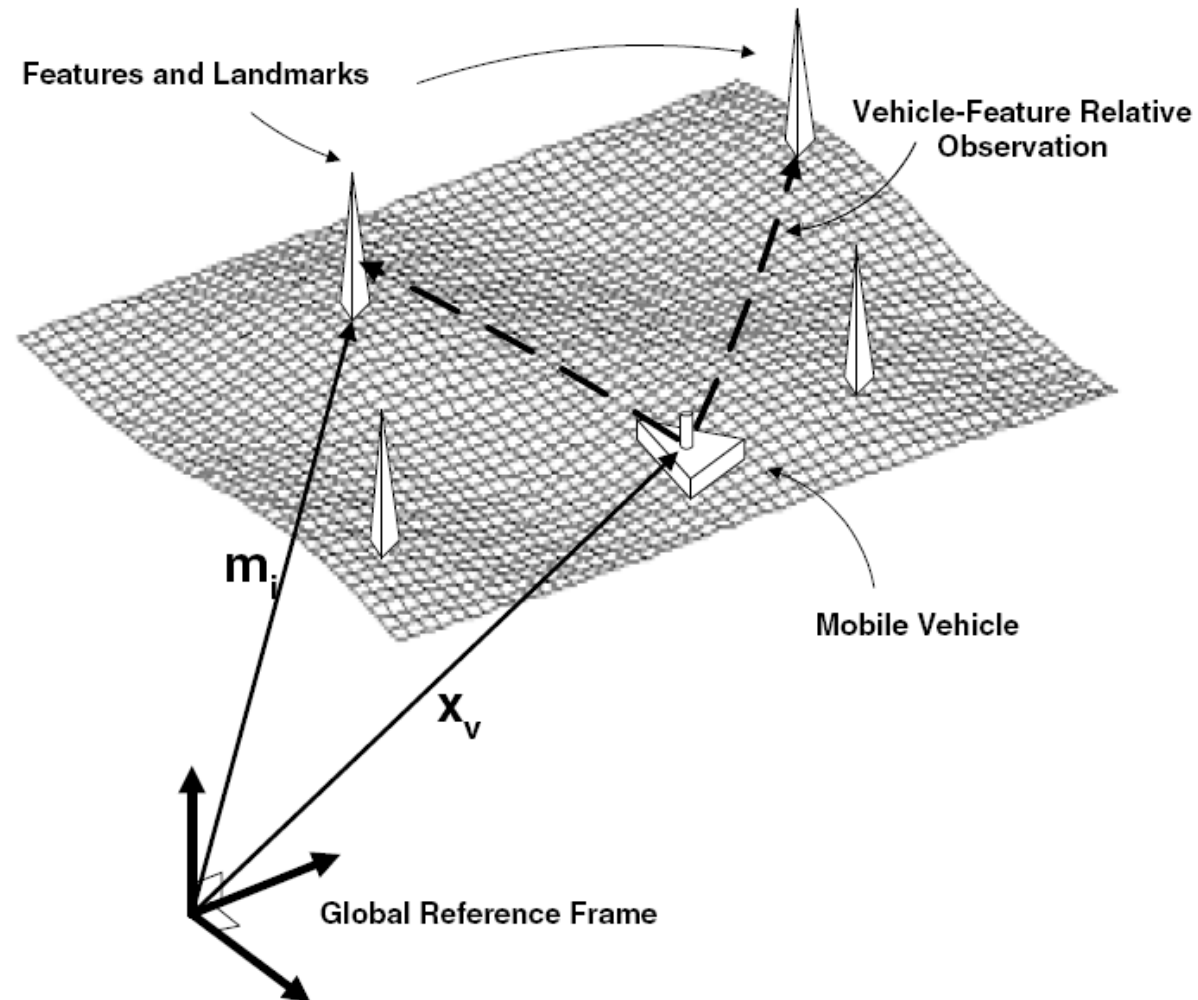
- The robot's controls
- Observations of nearby features

Estimate:

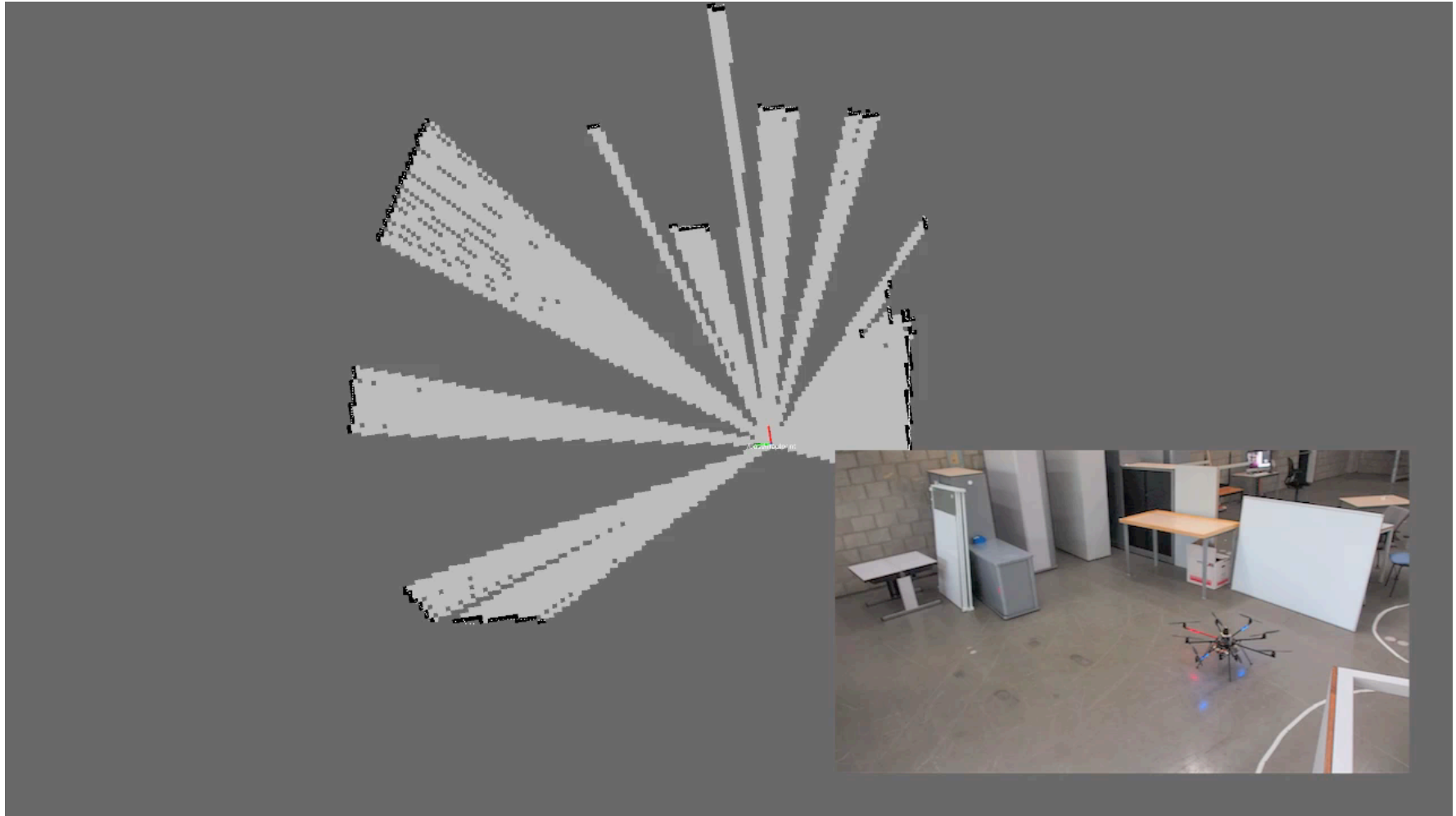
- Map of features
- Path of the robot



Structure of the Landmark-based SLAM-Problem



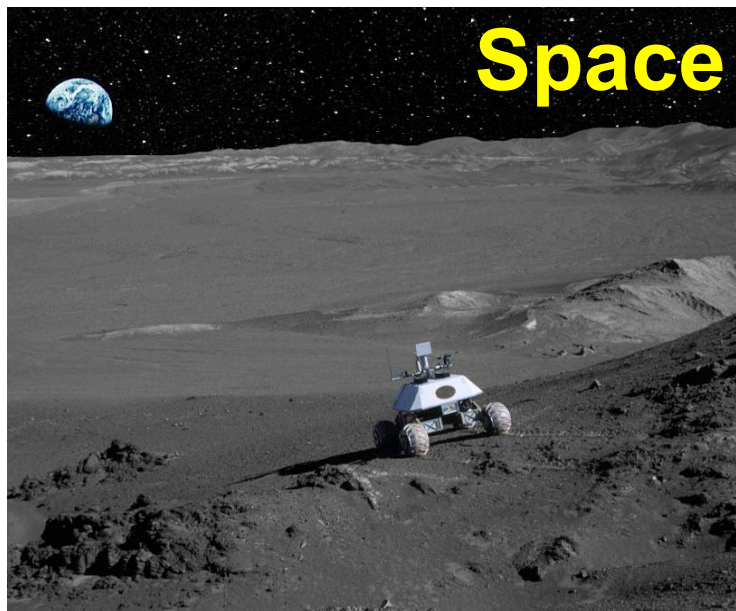
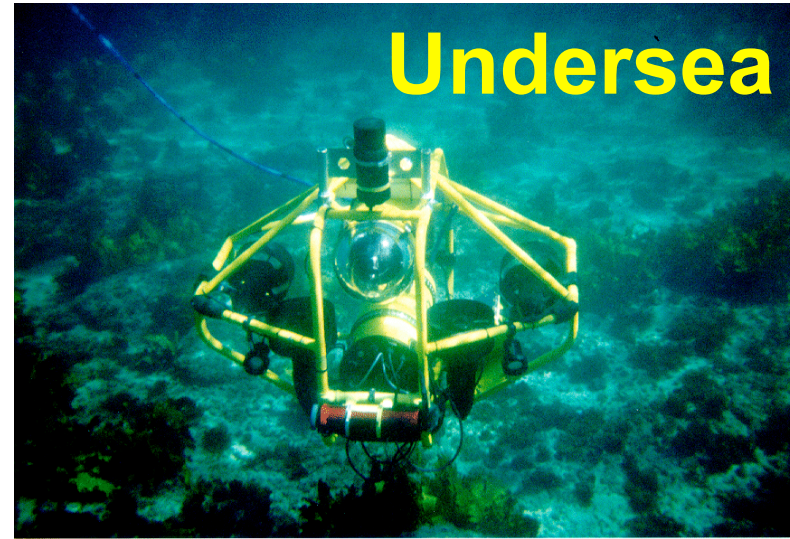
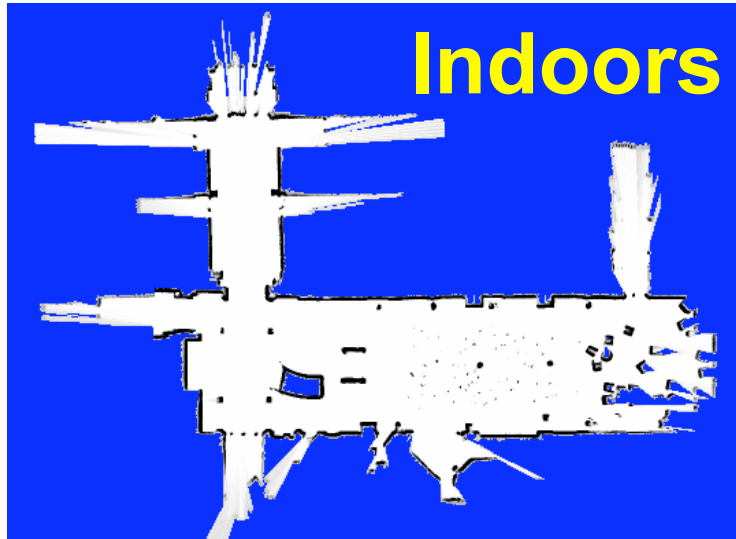
3D SLAM example – Hector SLAM



3D SLAM example – Octo SLAM

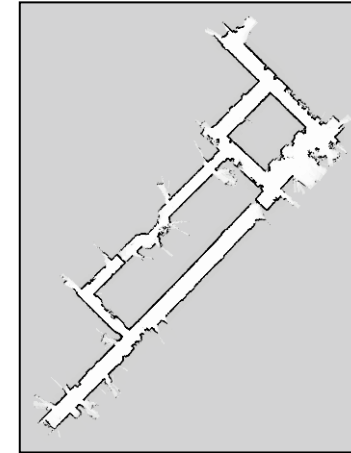
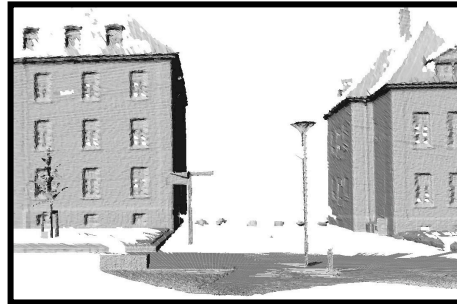
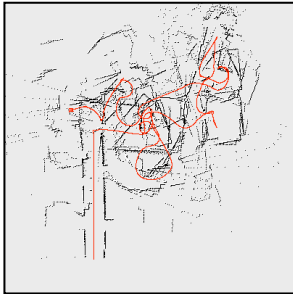


SLAM Applications



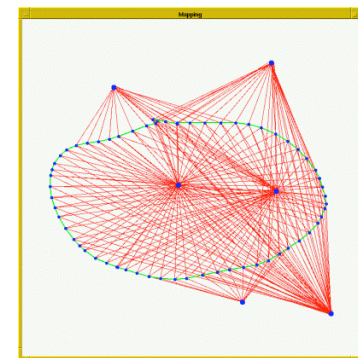
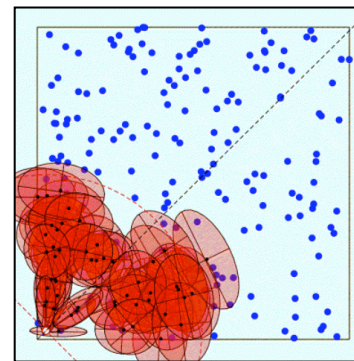
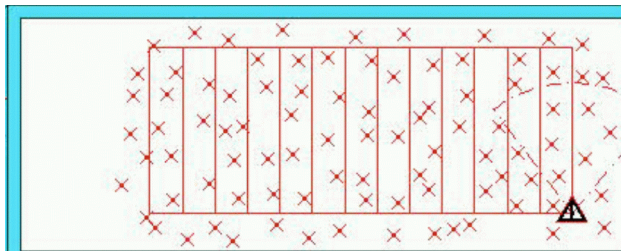
Representations

- Grid maps or scans



[Lu & Milios, 97; Gutmann, 98; Thrun 98; Burgard, 99; Konolige & Gutmann, 00; Thrun, 00; Arras, 99; Haehnel, 01;...]

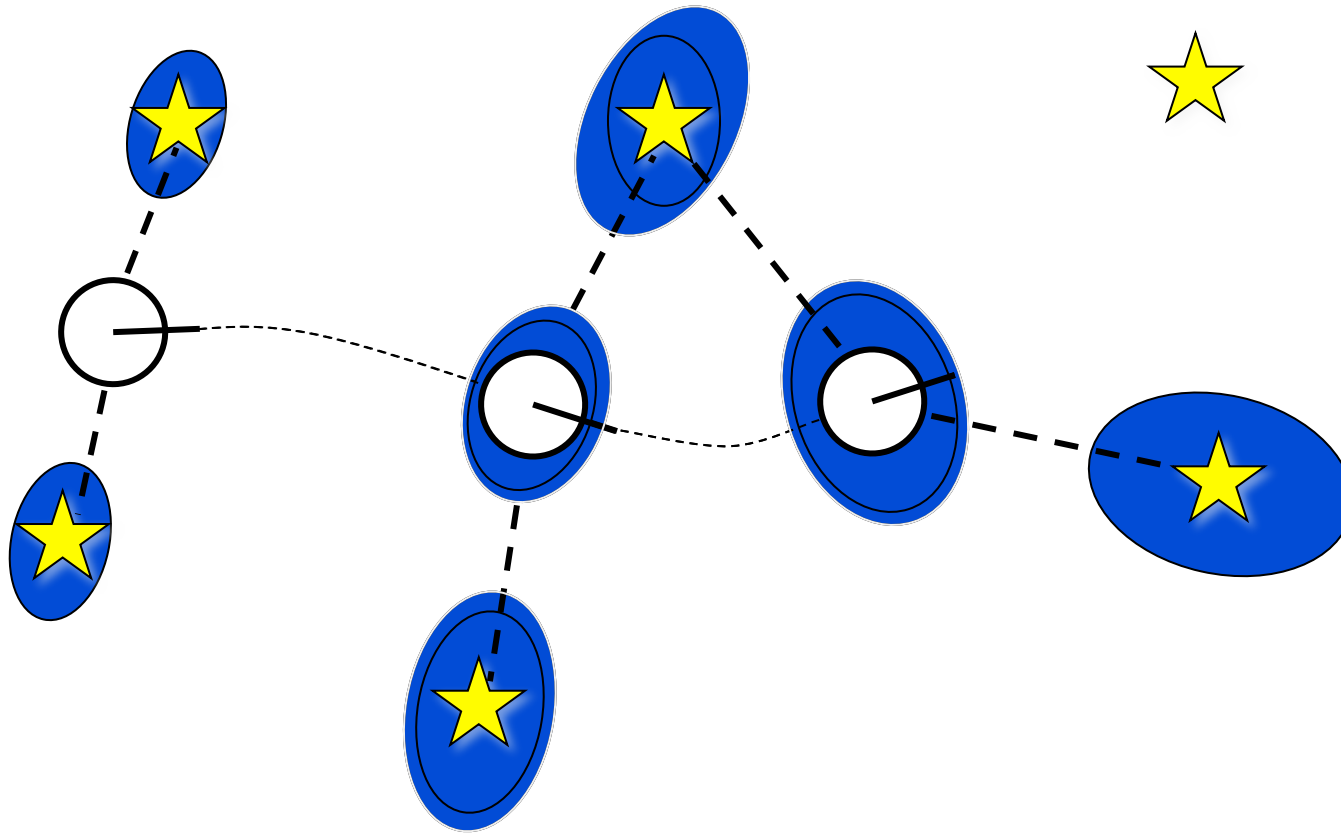
- Landmark-based



[Leonard et al., 98; Castelanos et al., 99; Dissanayake et al., 2001; Montemerlo et al., 2002;...]

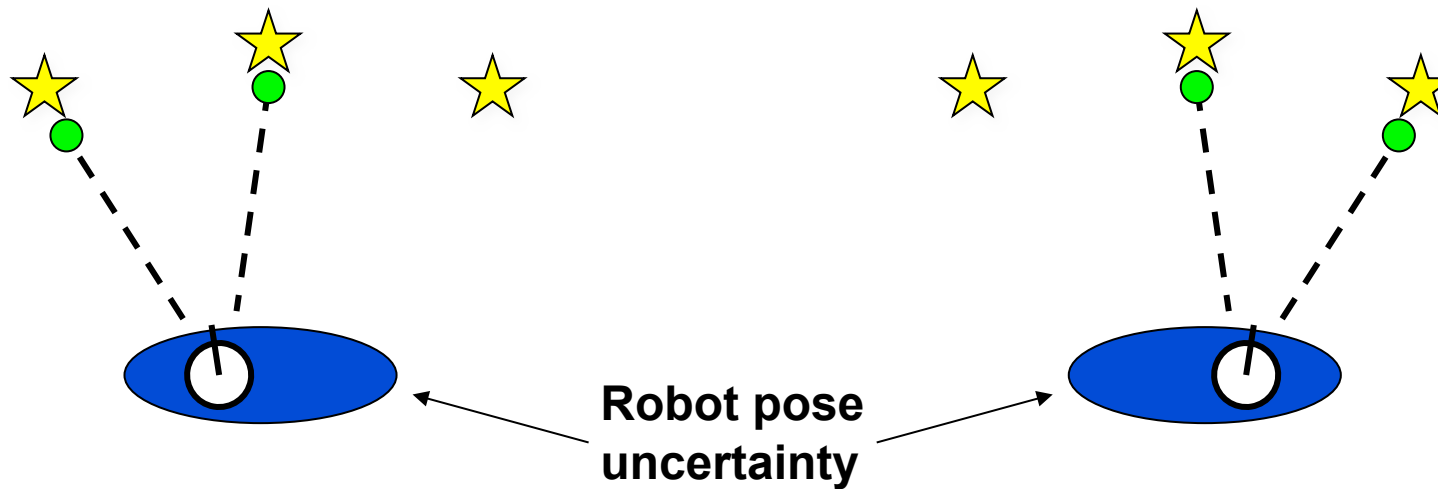
Why is SLAM a hard problem?

SLAM: robot path and map are both **unknown**



Robot path error correlates errors in the map

Why is SLAM a hard problem?



- In the real world, the mapping between observations and landmarks is unknown
- Picking wrong data associations can have catastrophic consequences
- Pose error correlates data associations

SLAM: Simultaneous Localization and Mapping

- Full SLAM: Estimates entire path and map!

$$p(x_{1:t}, m \mid z_{1:t}, u_{1:t})$$

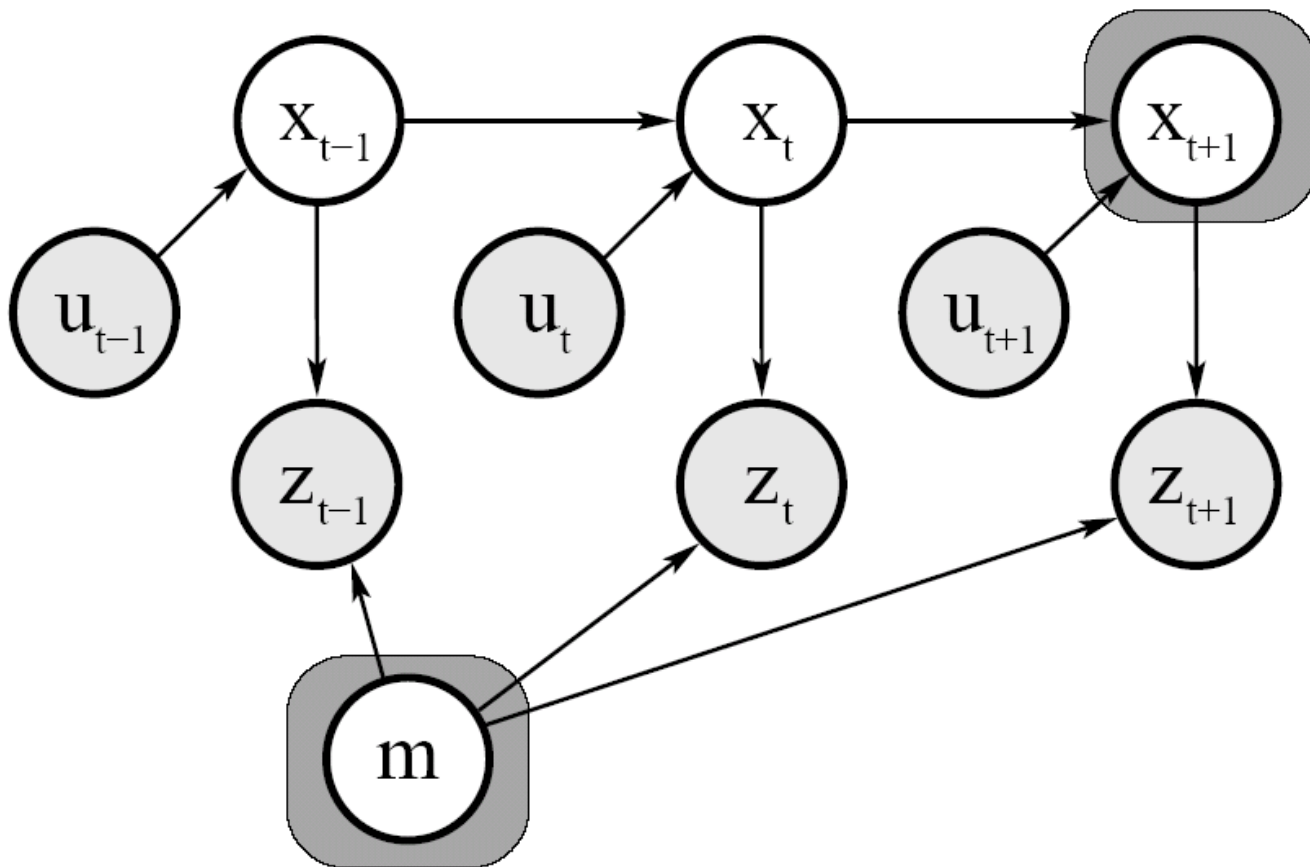
- Online SLAM:

$$p(x_t, m \mid z_{1:t}, u_{1:t}) = \int \int \dots \int p(x_{1:t}, m \mid z_{1:t}, u_{1:t}) dx_1 dx_2 \dots dx_{t-1}$$

Integrations typically done one at a time

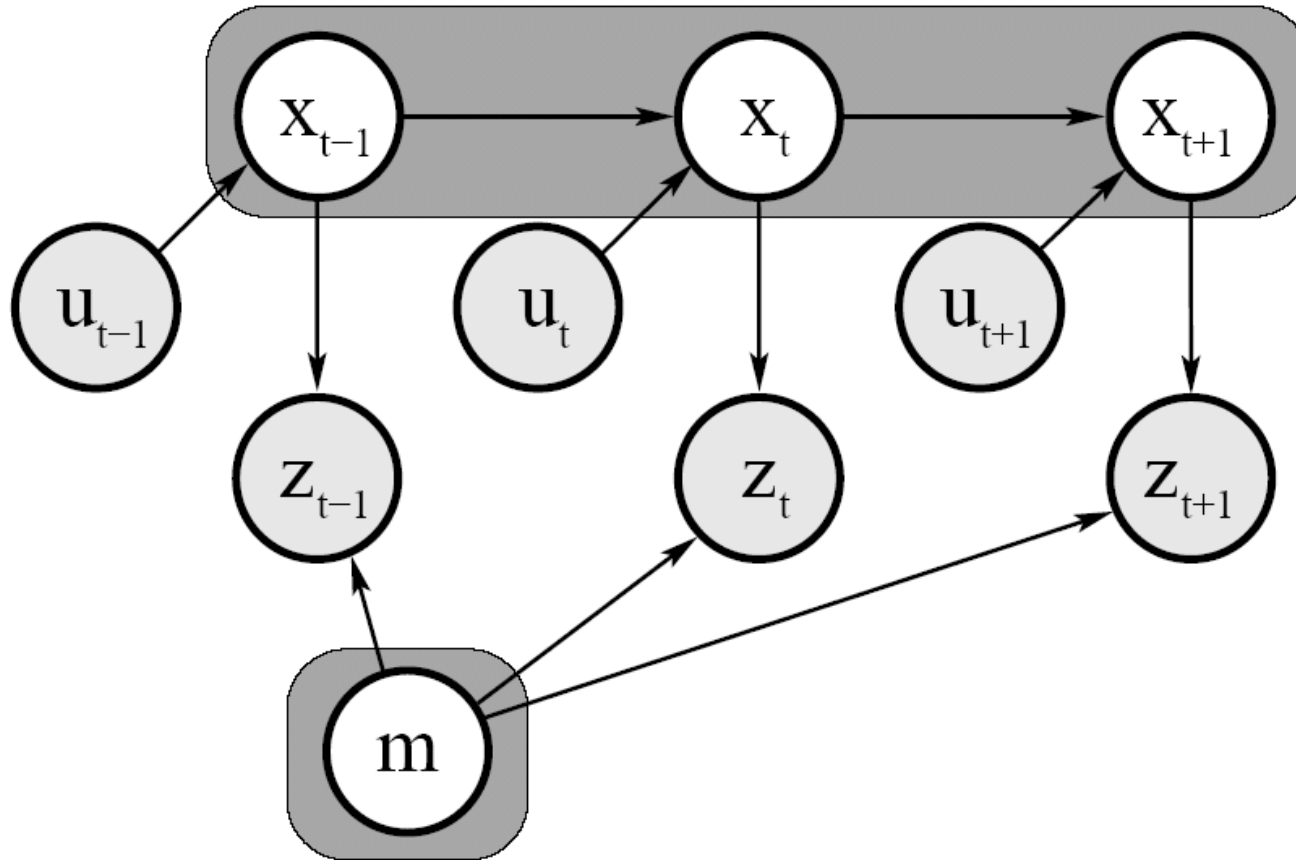
Estimates most recent pose and map!

Graphical Model of Online SLAM:



$$p(x_t, m \mid z_{1:t}, u_{1:t}) = \int \int \dots \int p(x_{1:t}, m \mid z_{1:t}, u_{1:t}) dx_1 dx_2 \dots dx_{t-1}$$

Graphical Model of Full SLAM:



$$p(x_{1:t}, m \mid z_{1:t}, u_{1:t})$$

Techniques for Generating Consistent Maps

- Scan matching
- EKF SLAM
- Fast-SLAM
- Probabilistic mapping with a single map and a posterior about poses
Mapping + Localization
- Graph-SLAM, SEIFs

Kalman Filter Algorithm

1. Algorithm **Kalman_filter**($\mu_{t-1}, \Sigma_{t-1}, u_t, z_t$):
2. Prediction:
3. $\bar{\mu}_t = A_t \mu_{t-1} + B_t u_t$
4. $\bar{\Sigma}_t = A_t \Sigma_{t-1} A_t^T + R_t$
5. Correction:
6. $K_t = \bar{\Sigma}_t C_t^T (C_t \bar{\Sigma}_t C_t^T + Q_t)^{-1}$
7. $\mu_t = \bar{\mu}_t + K_t (z_t - C_t \bar{\mu}_t)$
8. $\Sigma_t = (I - K_t C_t) \bar{\Sigma}_t$
9. Return μ_t, Σ_t

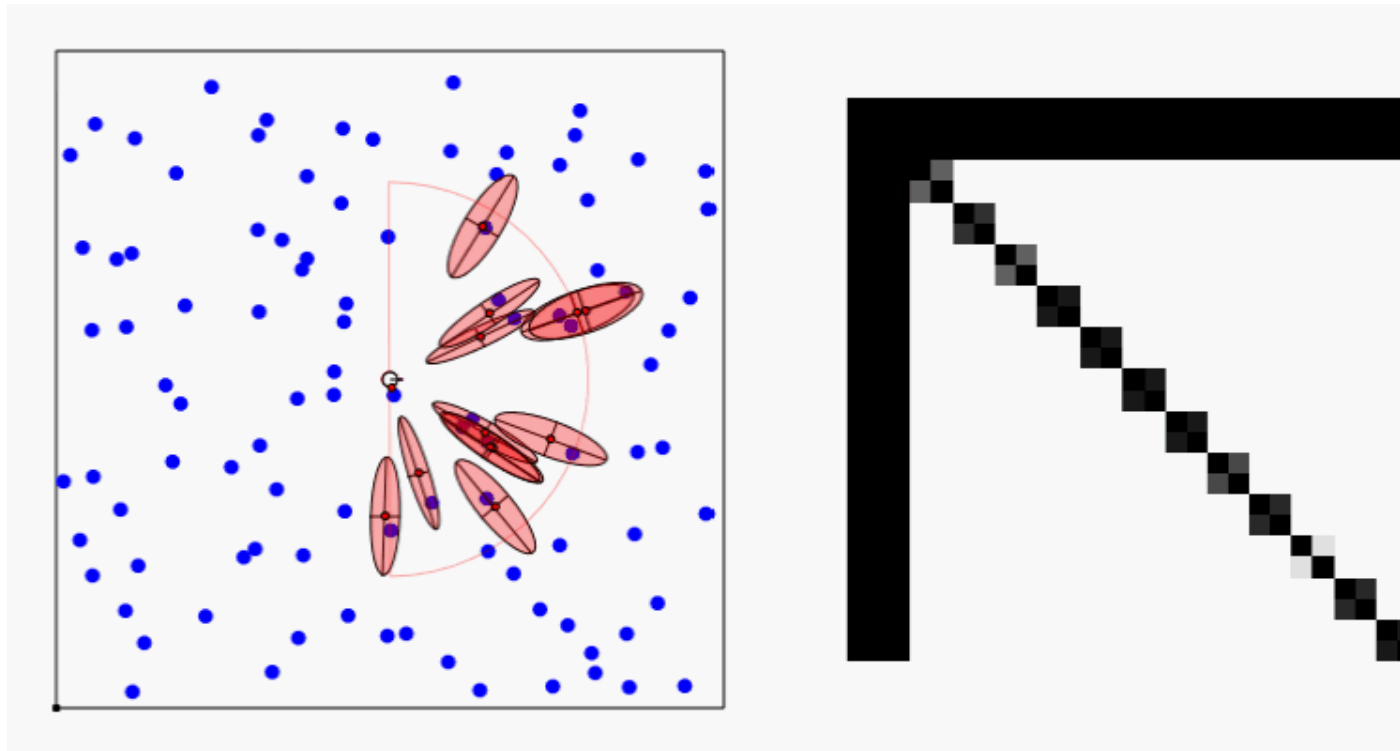
(E)KF-SLAM

- Map with N landmarks: (3+2N)-dimensional Gaussian

$$Bel(x_t, m_t) = \begin{pmatrix} x \\ y \\ \theta \\ l_1 \\ l_2 \\ \vdots \\ l_N \end{pmatrix}, \begin{pmatrix} \sigma_x^2 & \sigma_{xy} & \sigma_{x\theta} & \sigma_{xl_1} & \sigma_{xl_2} & \cdots & \sigma_{xl_N} \\ \sigma_{xy} & \sigma_y^2 & \sigma_{y\theta} & \sigma_{yl_1} & \sigma_{yl_2} & \cdots & \sigma_{yl_N} \\ \sigma_{x\theta} & \sigma_{y\theta} & \sigma_\theta^2 & \sigma_{\theta l_1} & \sigma_{\theta l_2} & \cdots & \sigma_{\theta l_N} \\ \sigma_{xl_1} & \sigma_{yl_1} & \sigma_{\theta l_1} & \sigma_{l_1}^2 & \sigma_{l_1 l_2} & \cdots & \sigma_{l_1 l_N} \\ \sigma_{xl_2} & \sigma_{yl_2} & \sigma_{\theta l_2} & \sigma_{l_1 l_2} & \sigma_{l_2}^2 & \cdots & \sigma_{l_2 l_N} \\ \vdots & \vdots & \vdots & \vdots & \vdots & \ddots & \vdots \\ \sigma_{xl_N} & \sigma_{yl_N} & \sigma_{\theta l_N} & \sigma_{l_1 l_N} & \sigma_{l_2 l_N} & \cdots & \sigma_{l_N}^2 \end{pmatrix}$$

- Can handle hundreds of dimensions

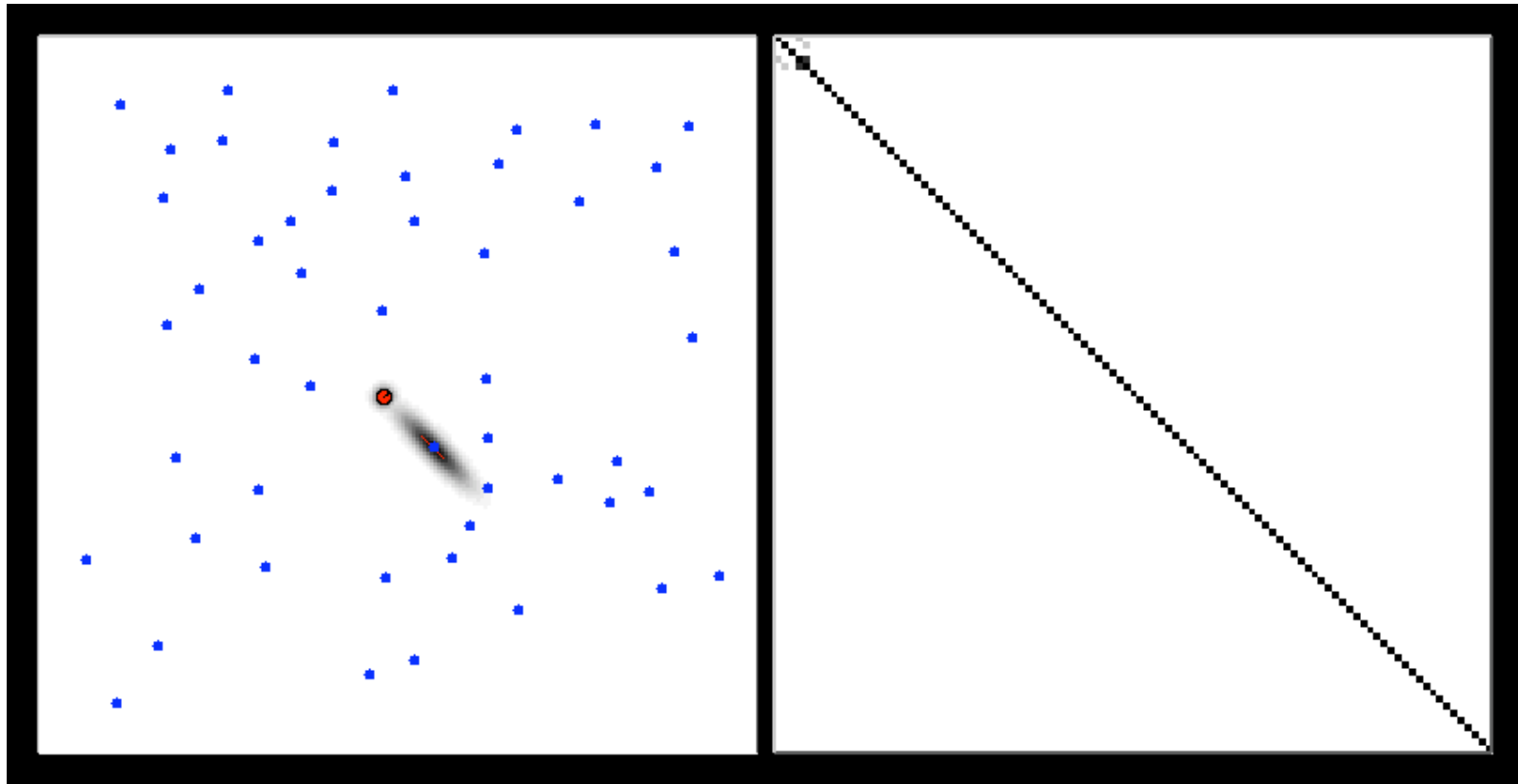
Classical Solution – The EKF



Blue path = true path Red path = estimated path Black path = odometry

- Approximate the SLAM posterior with a high-dimensional Gaussian [Smith & Cheesman, 1986] ...
- **Single hypothesis data association**

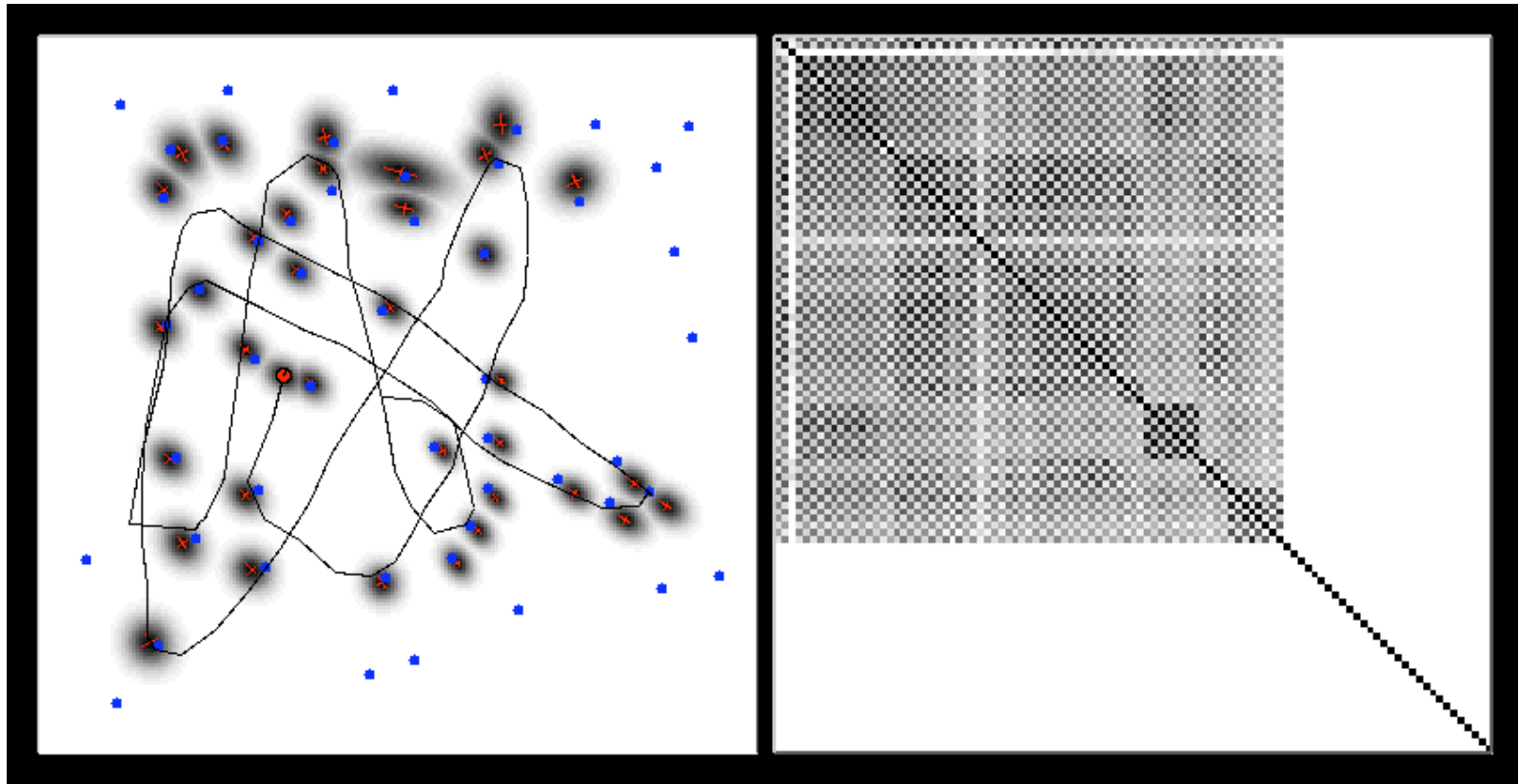
EKF-SLAM



Map

Correlation matrix

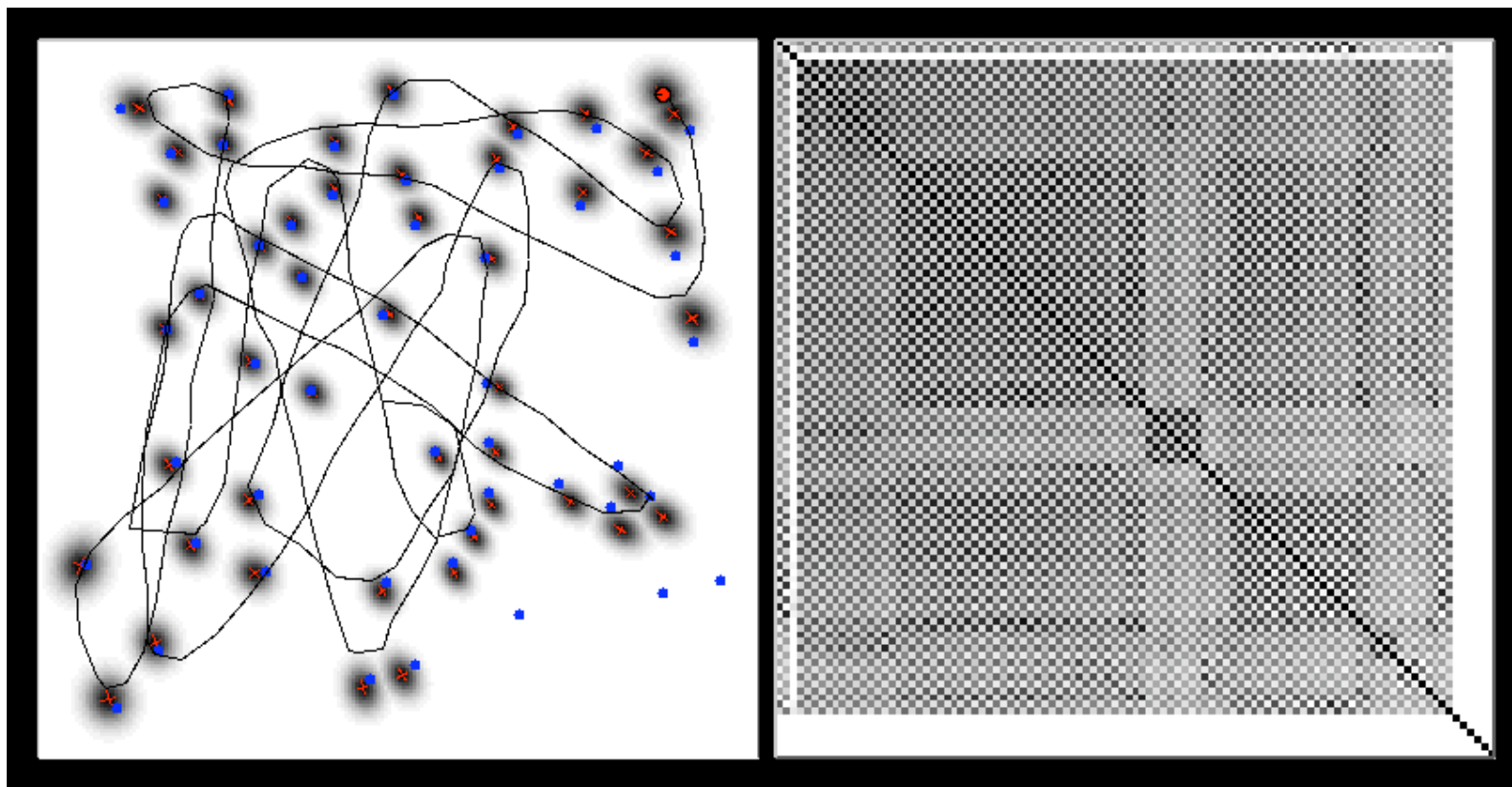
EKF-SLAM



Map

Correlation matrix

EKF-SLAM



Map

Correlation matrix

Victoria Park Data Set



[courtesy by E. Nebot]

Victoria Park Data Set Vehicle



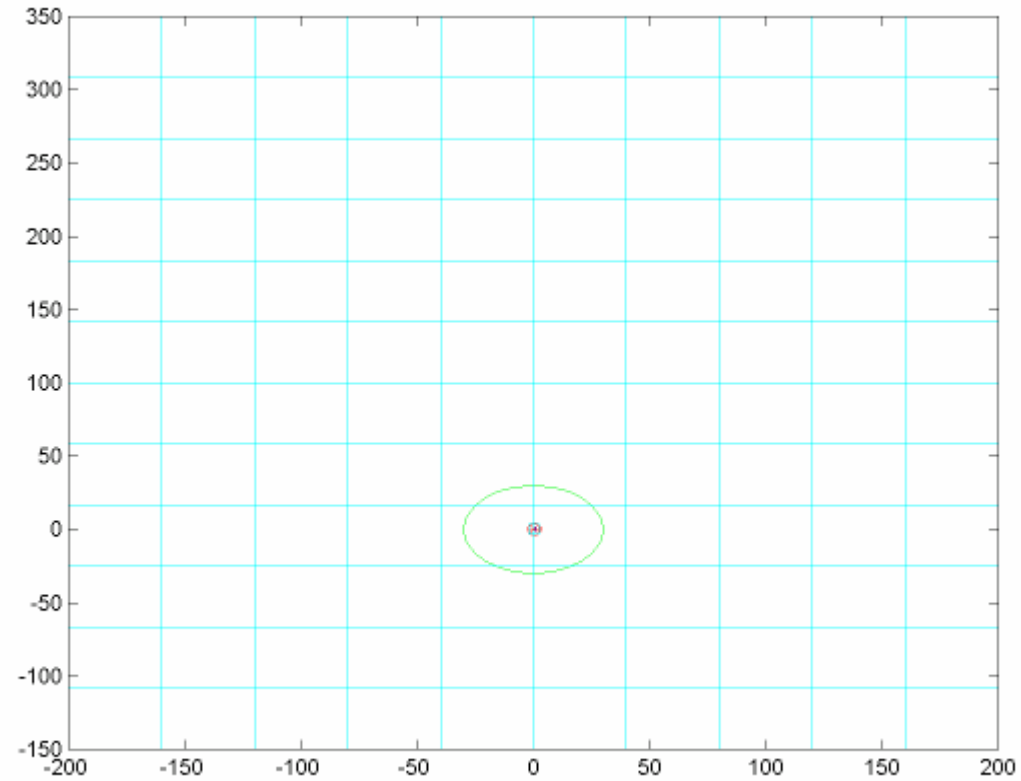
[courtesy by E. Nebot]

Data Acquisition



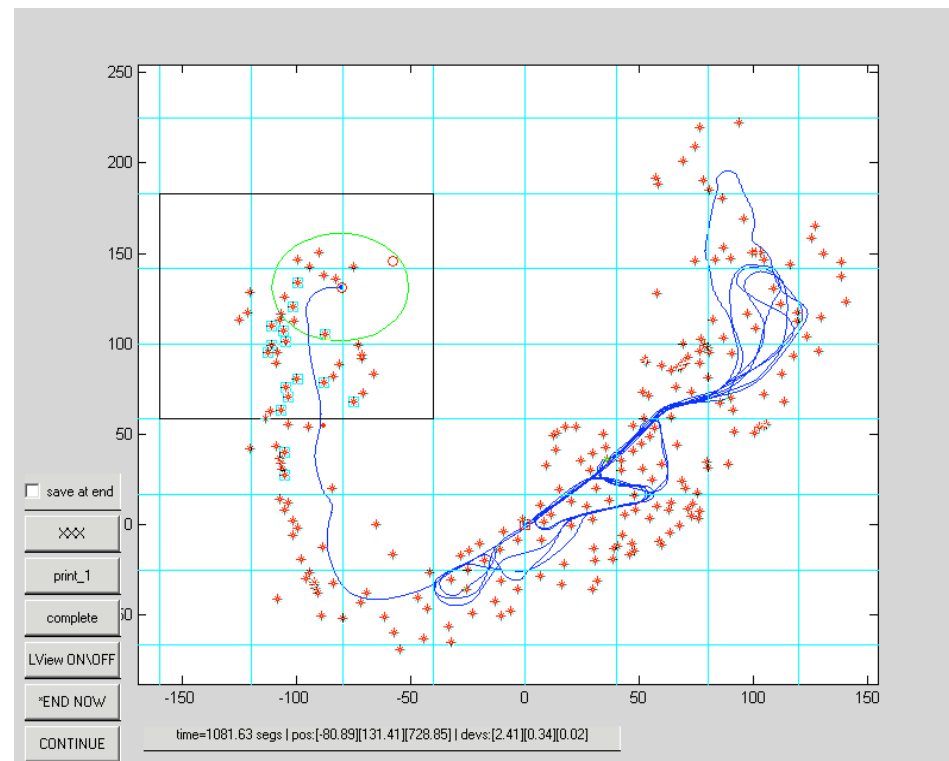
[courtesy by E. Nebot]

SLAM



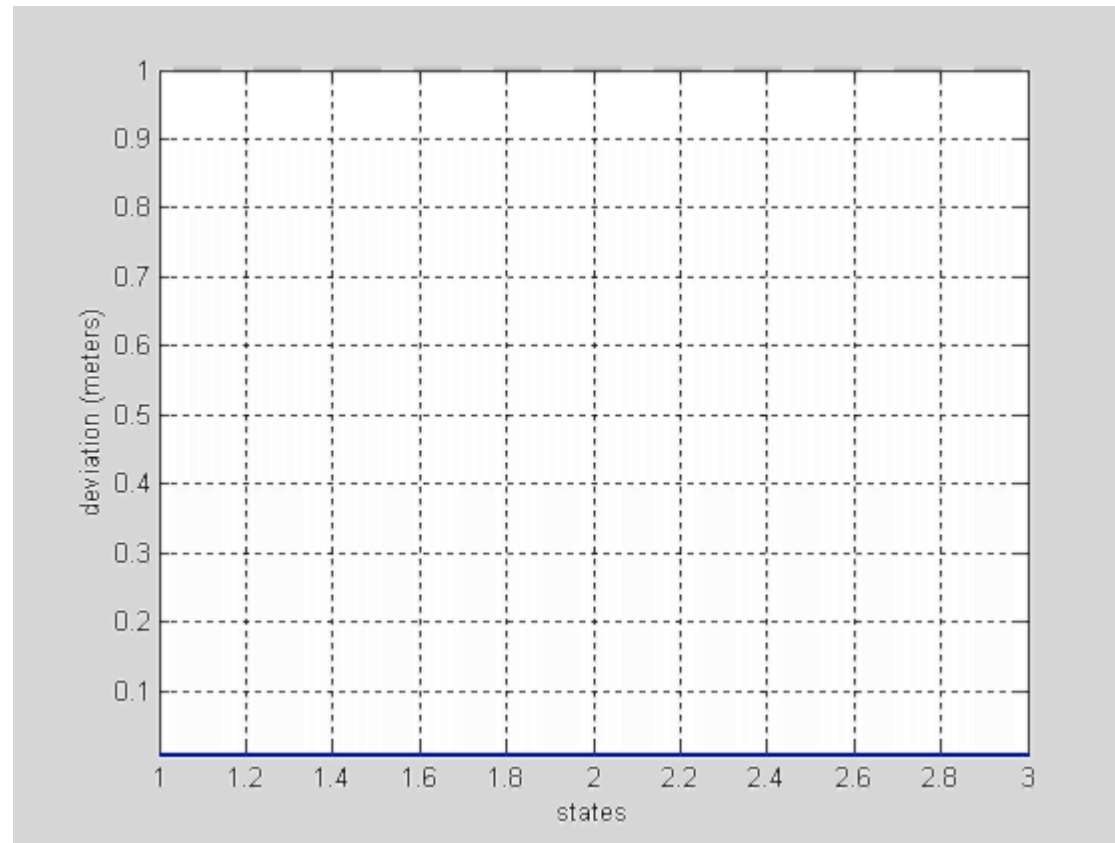
[courtesy by E. Nebot]

Map and Trajectory



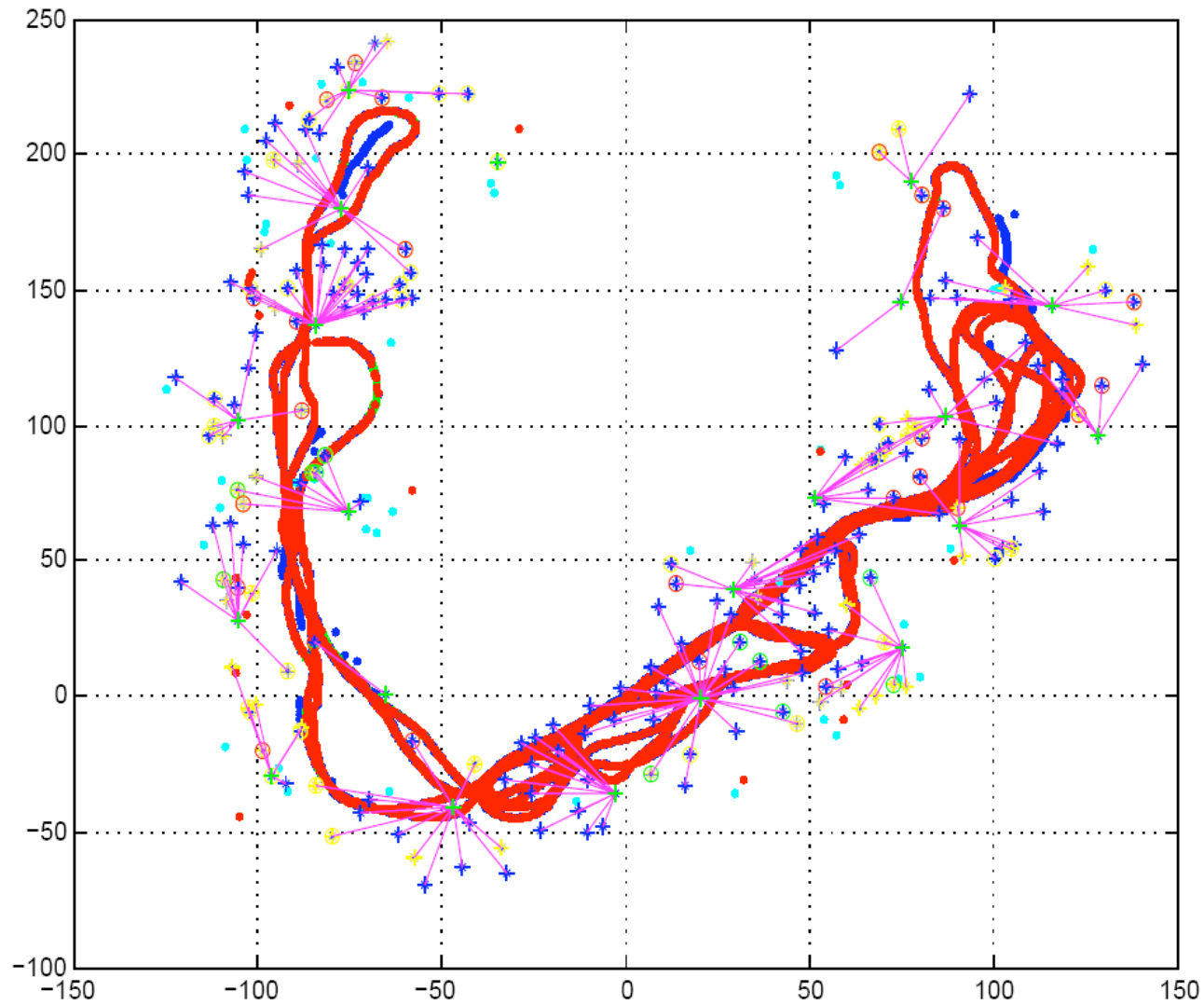
[courtesy by E. Nebot]

Landmark Covariance



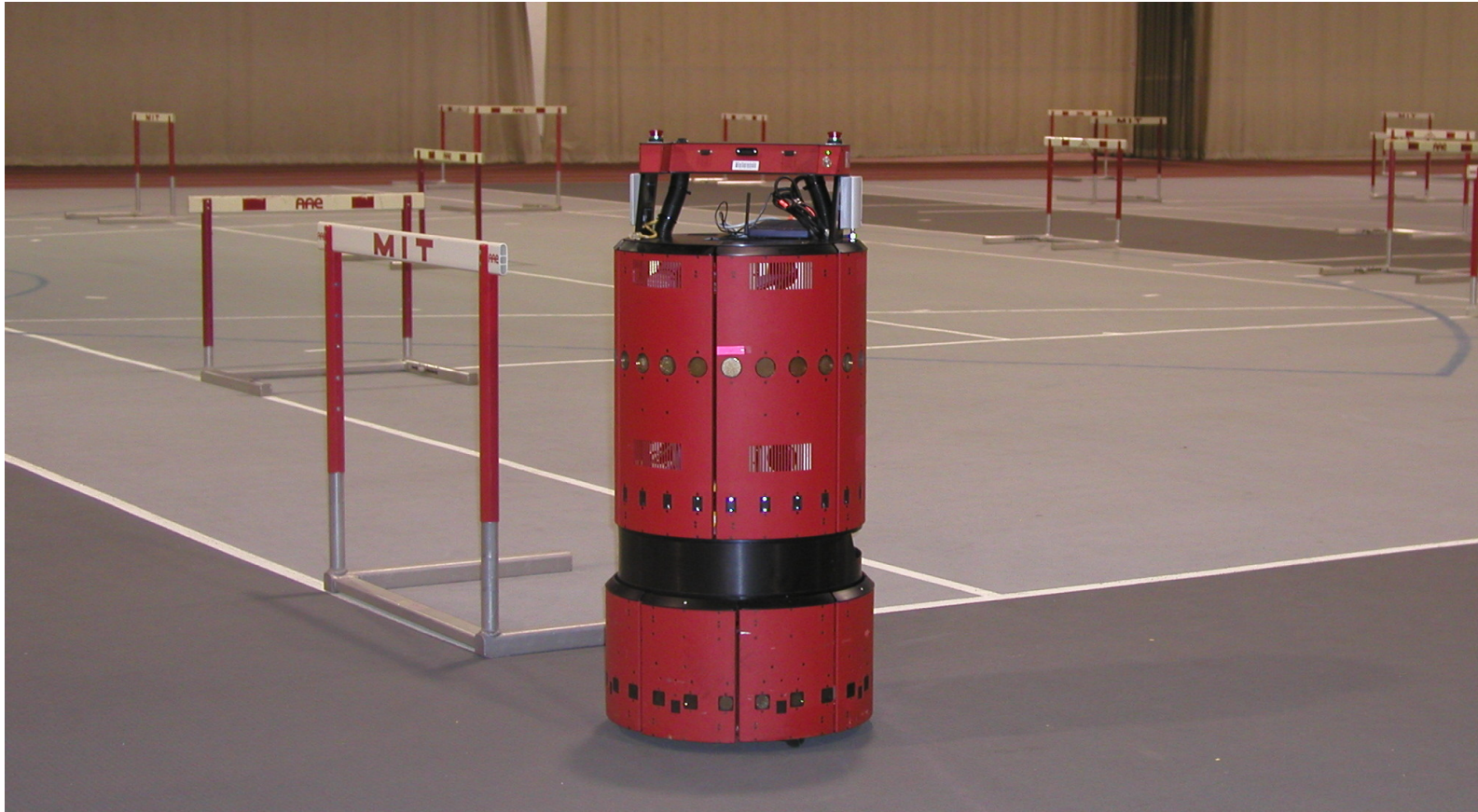
[courtesy by E. Nebot]

Estimated Trajectory



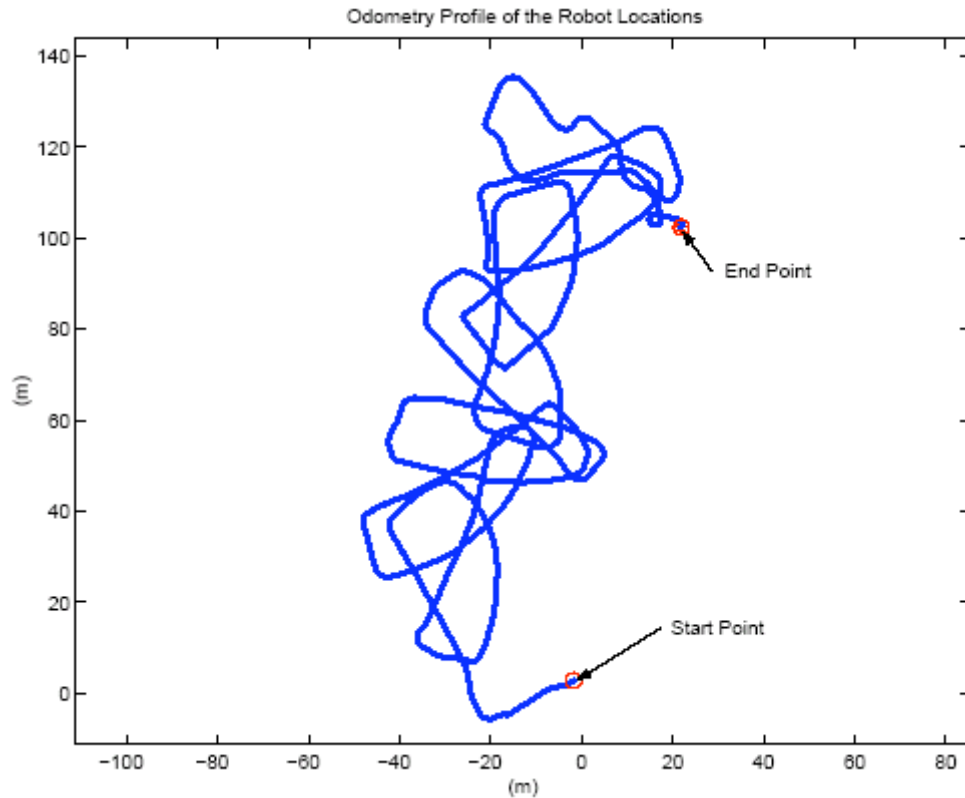
[courtesy by E. Nebot]

EKF SLAM Application

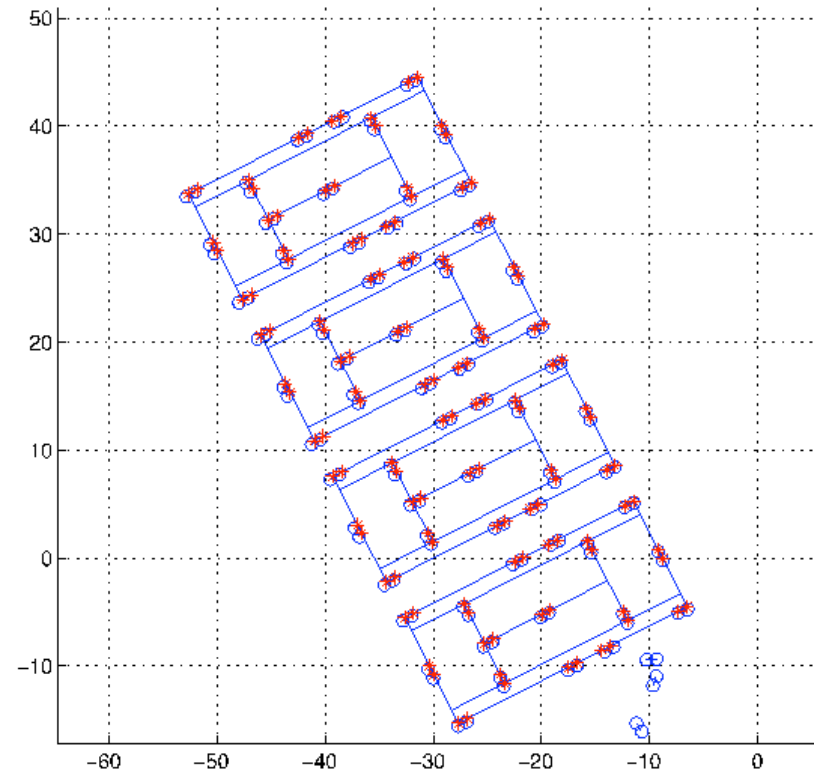


[courtesy by John Leonard]

EKF SLAM Application



odometry



estimated trajectory

Approximations for SLAM

- Local submaps
[Leonard et al.99, Bosse et al. 02, Newman et al. 03]
- Sparse links (correlations)
[Lu & Milios 97, Guivant & Nebot 01]
- Sparse extended information filters
[Frese et al. 01, Thrun et al. 02]
- Thin junction tree filters
[Paskin 03]
- Rao-Blackwellisation (FastSLAM)
[Murphy 99, Montemerlo et al. 02, Eliazar et al. 03, Haehnel et al. 03]

EKF-SLAM Summary

- Quadratic in the number of landmarks: $O(n^2)$
- Convergence results for the linear case.
- Can **diverge** if nonlinearities are large!
- Have been applied successfully in large-scale environments.
- Approximations reduce the computational complexity.